

INSTRUCTIONS TO CANDIDATES

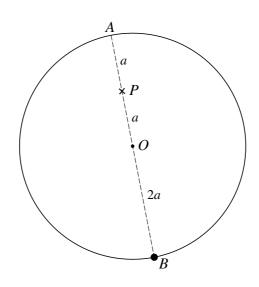
- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet.
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer all the questions.
- Do **not** write in the bar codes.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- The acceleration due to gravity is denoted by $g \,\mathrm{m}\,\mathrm{s}^{-2}$. Unless otherwise instructed, when a numerical value is needed, use g = 9.8.
- You are permitted to use a graphical calculator in this paper.

INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- You are reminded of the need for clear presentation in your answers.
- The total number of marks for this paper is 72.
- This document consists of 8 pages. Any blank pages are indicated.

- 1 A top is set spinning with initial angular speed 83 rad s^{-1} , and it slows down with constant angular deceleration. When it has turned through 1000 radians, its angular speed is 67 rad s⁻¹.
 - (i) Find the angular deceleration of the top. [2]
 - (ii) Find the time taken, from the start, for the top to turn through 400 radians. [4]
- 2 The region *R* is bounded by the *x*-axis, the lines x = a and x = 2a, and the curve $y = \frac{a^3}{x^2}$ for $a \le x \le 2a$, where *a* is a positive constant. A uniform solid of revolution is formed by rotating *R* through 2π radians about the *x*-axis. Find the *x*-coordinate of the centre of mass of this solid. [7]



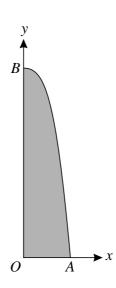


A uniform circular disc has mass 4m, radius 2a and centre O. The points A and B are at opposite ends of a diameter of the disc, and the mid-point of OA is P. A particle of mass m is attached to the disc at B. The resulting compound pendulum is in a vertical plane and is free to rotate about a fixed horizontal axis passing through P and perpendicular to the disc (see diagram). The pendulum makes small oscillations.

- (i) Find the moment of inertia of the pendulum about the axis. [4]
- (ii) Find the approximate period of the small oscillations.

[4]

- 4 From a helicopter, a small plane is spotted 3750 m away on a bearing of 075° . The plane is at the same altitude as the helicopter, and is flying with constant speed 62 m s^{-1} in a horizontal straight line on a bearing of 295°. The helicopter flies with constant speed 48 m s^{-1} in a straight line, and intercepts the plane.
 - (i) Find the bearings of the two possible directions in which the helicopter could fly. [5]
 - (ii) Given that interception occurs in the shorter of the two possible times, find the time taken to make the interception. [4]

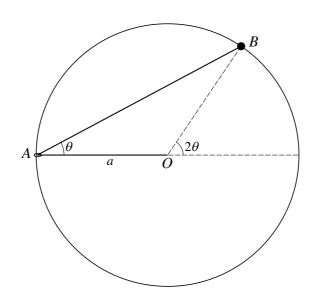


A uniform lamina of mass 63 kg occupies the region bounded by the *x*-axis, the *y*-axis, and the curve $y = 8 - x^3$ for $0 \le x \le 2$. The unit of length is the metre. The vertices of the lamina are O(0, 0), A(2, 0) and B(0, 8) (see diagram).

(i) Show that the moment of inertia of this lamina about OB is 56 kg m². [6]

It is given that the moment of inertia of the lamina about OA is 1036.8 kg m², and the centre of mass of the lamina has coordinates $(\frac{4}{5}, \frac{24}{7})$. The lamina is free to rotate in a vertical plane about a fixed horizontal axis passing through O and perpendicular to the lamina. Starting with the lamina at rest with B vertically above O, a couple of constant anticlockwise moment 800 N m is applied to the lamina.

- (ii) Show that the lamina begins to rotate anticlockwise. [2]
- (iii) Find the angular speed of the lamina at the instant when *OB* first becomes horizontal. [6]

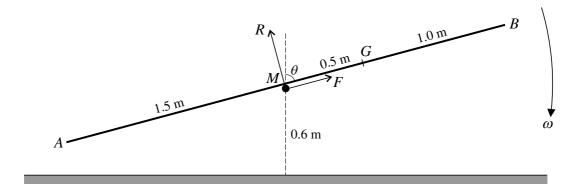


A smooth circular wire, with centre *O* and radius *a*, is fixed in a vertical plane, and the point *A* is on the wire at the same horizontal level as *O*. A small bead *B* of mass *m* can move freely on the wire. A light elastic string, with natural length *a* and modulus of elasticity $\sqrt{3}mg$, passes through a fixed ring at *A*, and has one end fixed at *O* and the other end attached to *B*. The section *AB* of the string is at an angle θ above the horizontal, where $-\frac{1}{2}\pi < \theta < \frac{1}{2}\pi$, so that *OB* is at an angle 2 θ to the horizontal (see diagram).

(i) Taking *O* as the reference level for gravitational potential energy, show that the total potential energy of the system is

$$mga(\sqrt{3} + \sqrt{3}\cos 2\theta + \sin 2\theta).$$
 [4]

- (ii) Find the two values of θ for which the system is in equilibrium. [5]
- (iii) For each position of equilibrium, determine whether it is stable or unstable. [4]



A thin horizontal rail is fixed at a height of 0.6 m above horizontal ground. A non-uniform straight rod *AB* has mass 6 kg and length 3 m; its centre of mass *G* is 2 m from *A* and 1 m from *B*, and its moment of inertia about a perpendicular axis through its mid-point *M* is 4.9 kg m^2 . The rod is placed in a vertical plane perpendicular to the rail, with *A* on the ground and *M* in contact with the rail. It is released from rest in this position, and begins to rotate about *M*, without slipping on the rail. When the angle between *AB* and the upward vertical is θ radians, the rod has angular speed $\omega \text{ rad s}^{-1}$, the frictional force in the direction *AB* is *F* N, and the normal reaction is *R* N (see diagram).

(i) Show that
$$\omega^2 = 4.8 - 12 \cos \theta$$
. [3]

(ii) Find the angular acceleration of the rod in terms of
$$\theta$$
. [2]

- (iii) Show that $F = 94.8 \cos \theta 14.4$, and find R in terms of θ . [6]
- (iv) Given that the coefficient of friction between the rod and the rail is 0.9, show that the rod will slip on the rail before *B* hits the ground. [4]

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